

# Differential interferometry



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**Ph. Stee**

Observatoire de la Côte d'Azur

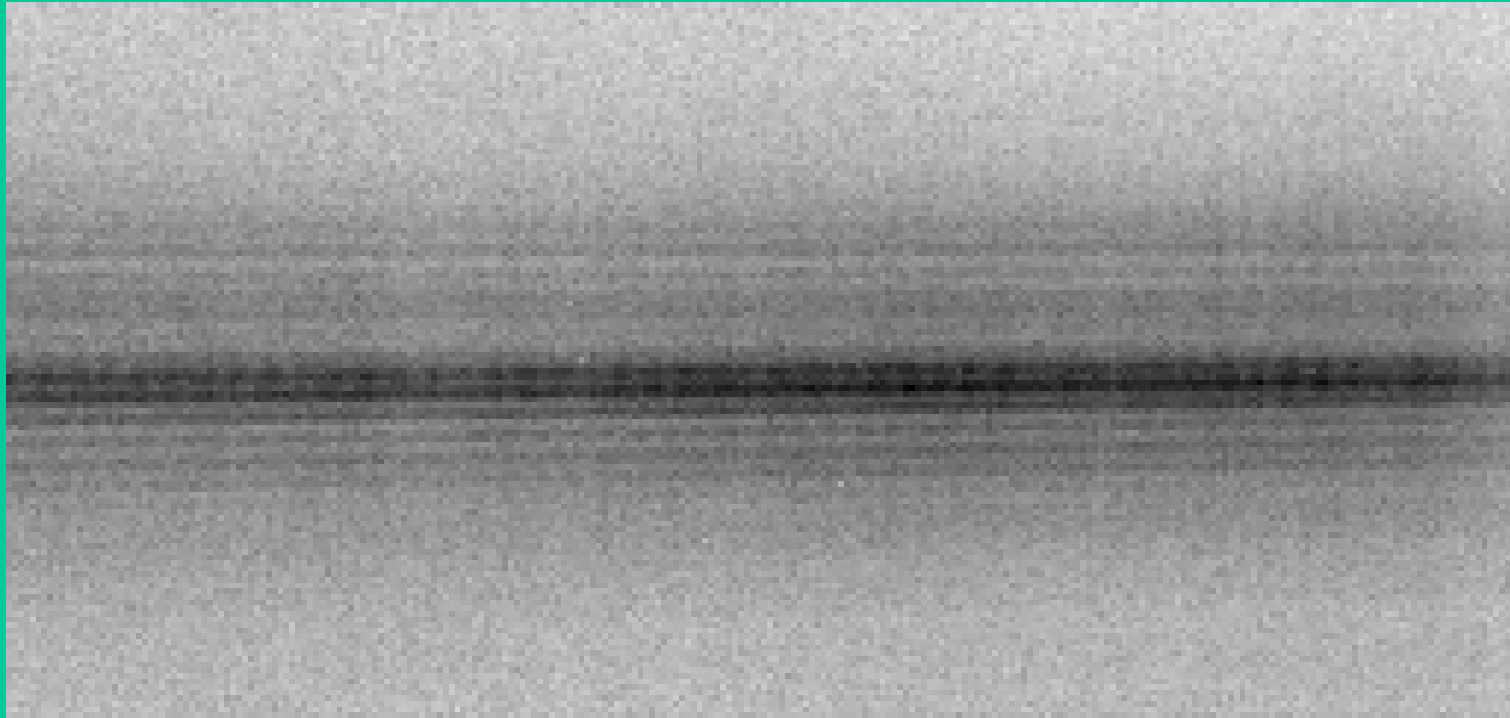
Département FRESNEL-Equipe GI2T

# Interferometry: fringe analysis



A field of Zebra

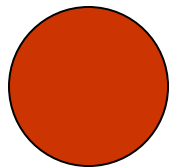
# *Fringes analysis ( $x-\lambda$ mode)*



**R Cas ( $V \approx 6$ ,  $K \approx -1.5$ )  $B = 14$  m - Dispersed Fringes in K band (GI2T).**

# Modulus of the visibility

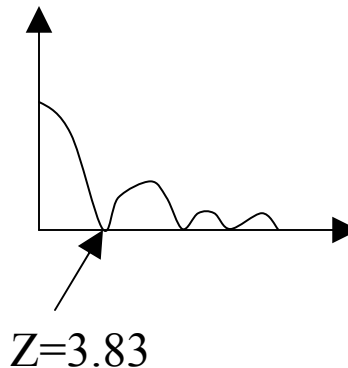
- Unresolved object (point source)  $V=1$



- Extended object  $V < 1$

For a circular object  $V = |2J_1(z)/z|$

$$B_r = 250 \lambda / \phi_{ud}$$



( $\lambda$  in  $\mu\text{m}$   $B_r$  in m,  $\phi$  in mas)

# How to define a stellar diameter ?

Not trivial !

Some definitions:

Optical radius: 
$$\tau(r) = \int_{r_0}^r K(r') \rho(r') dr' \approx 1$$

with  $K(r) = \kappa(r) + \sigma(r)$

Intensity radius:

$R_I = r$  with  $I(r)/I(0) \approx 0$

# Measure the temperature of a star

$$L = 4\pi R^2 \sigma T_{eff}^4$$

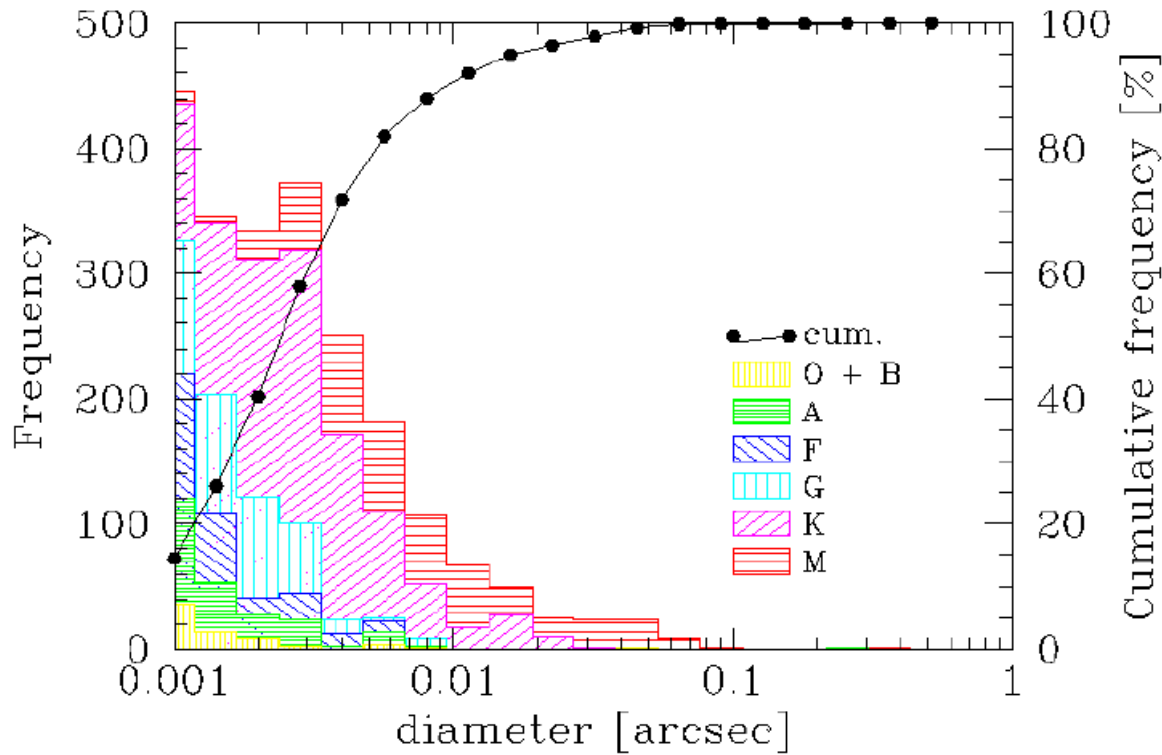
$$L = 4\pi d^2 f$$

$$\alpha = \frac{R}{d}$$

$$T_{eff}^4 = \frac{1}{\sigma} \frac{f}{\alpha^2}$$

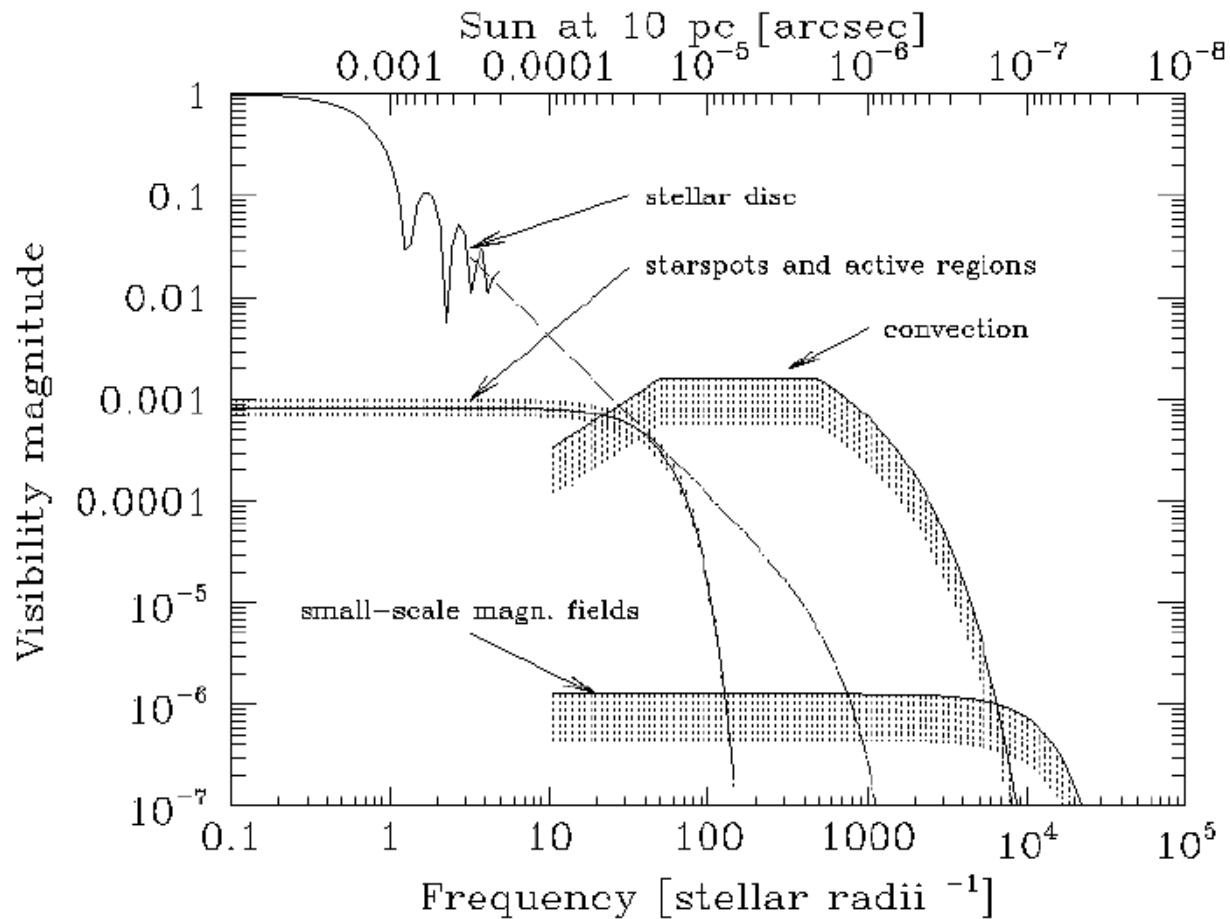
**Q: What is Teff ? ; -)**

# Diameter distribution of stars ?



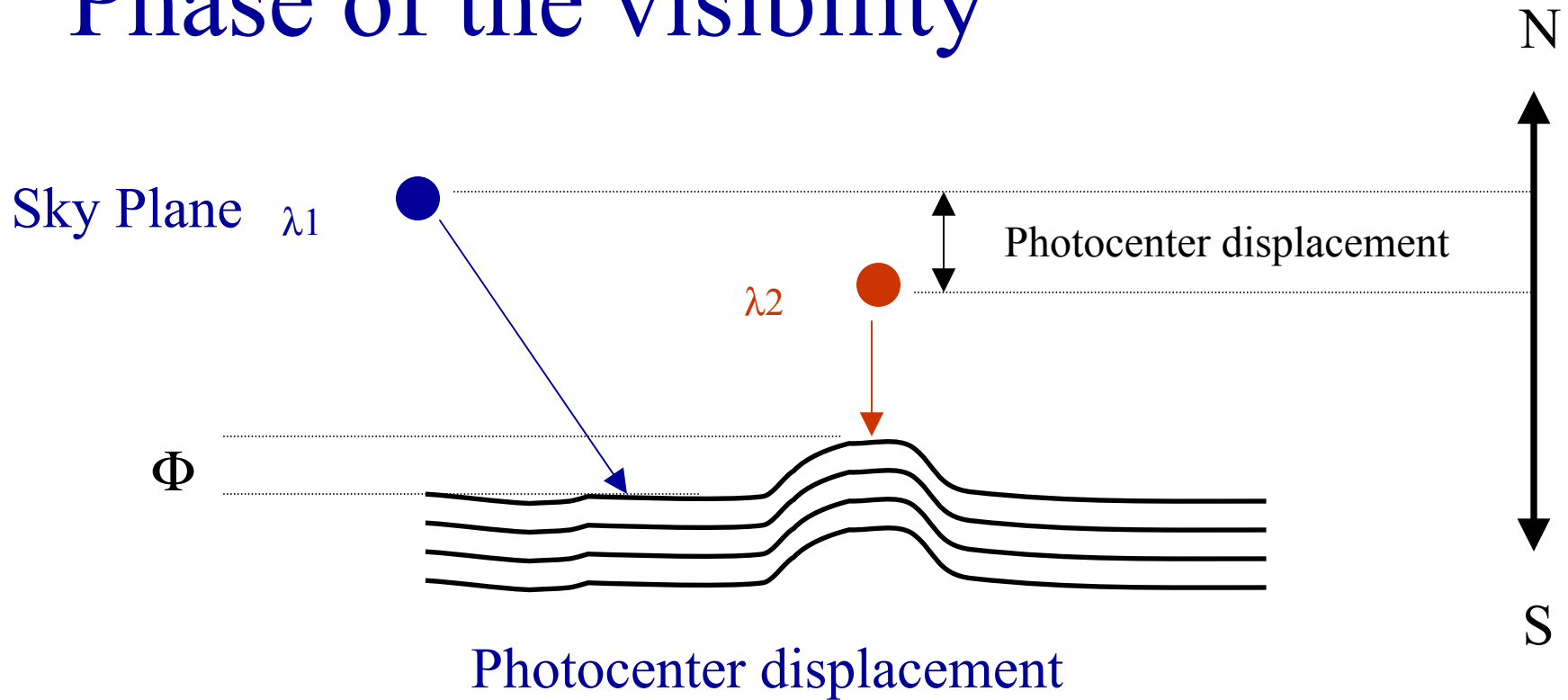
1309 sources  
50 % < 2.5 mas  
20 % > 5 mas  
7% > 10 mas -> UT

# What can be seen on a solar type star ( $1 R_m$ ) at 10 pc ?





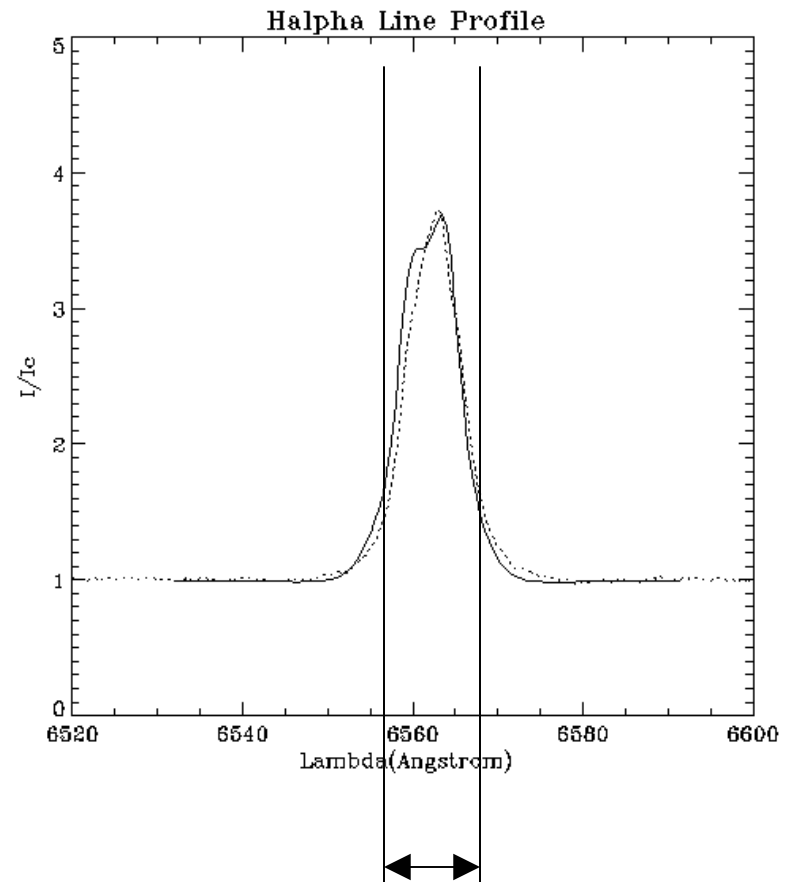
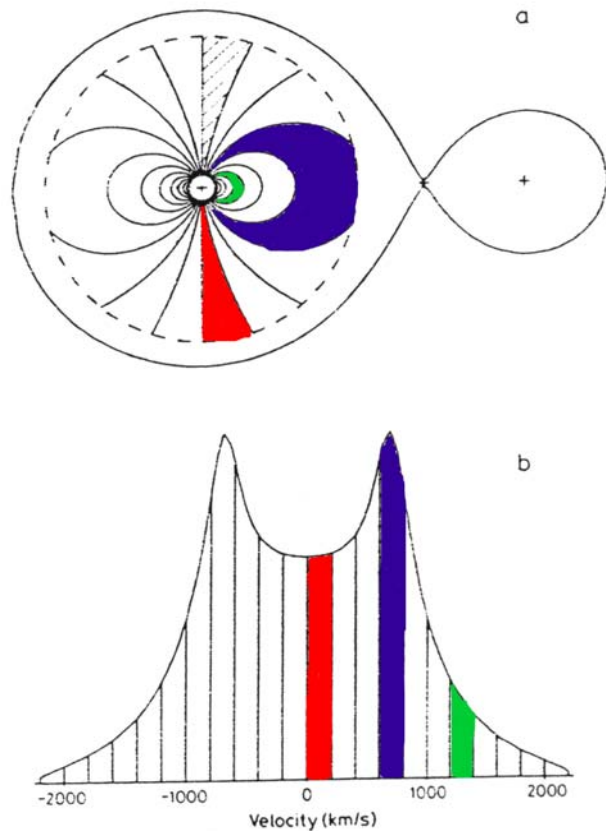
# Phase of the visibility



Shift of the fringes ( $\phi$ )

Change in the visibility phase

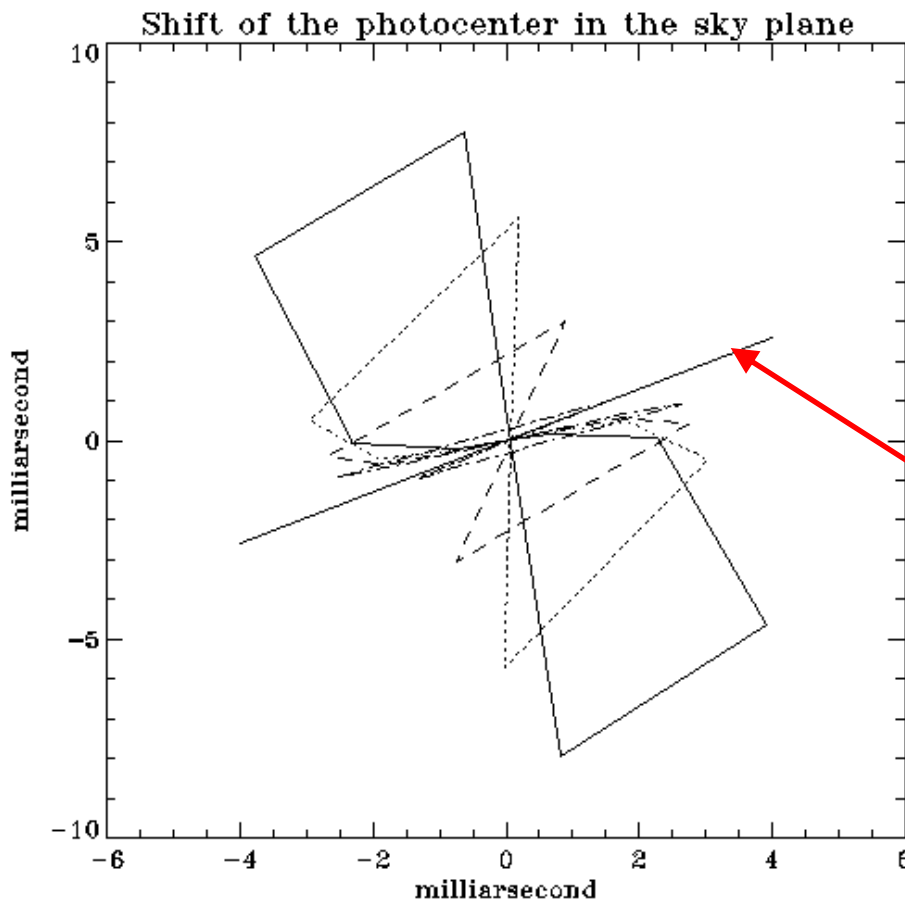
# Spectral filter = spatial filter



Line formation in a rotating envelope

MkIII filter: 10Å

# Photocenter displacement on the sky plane: $\phi=f(\lambda)$

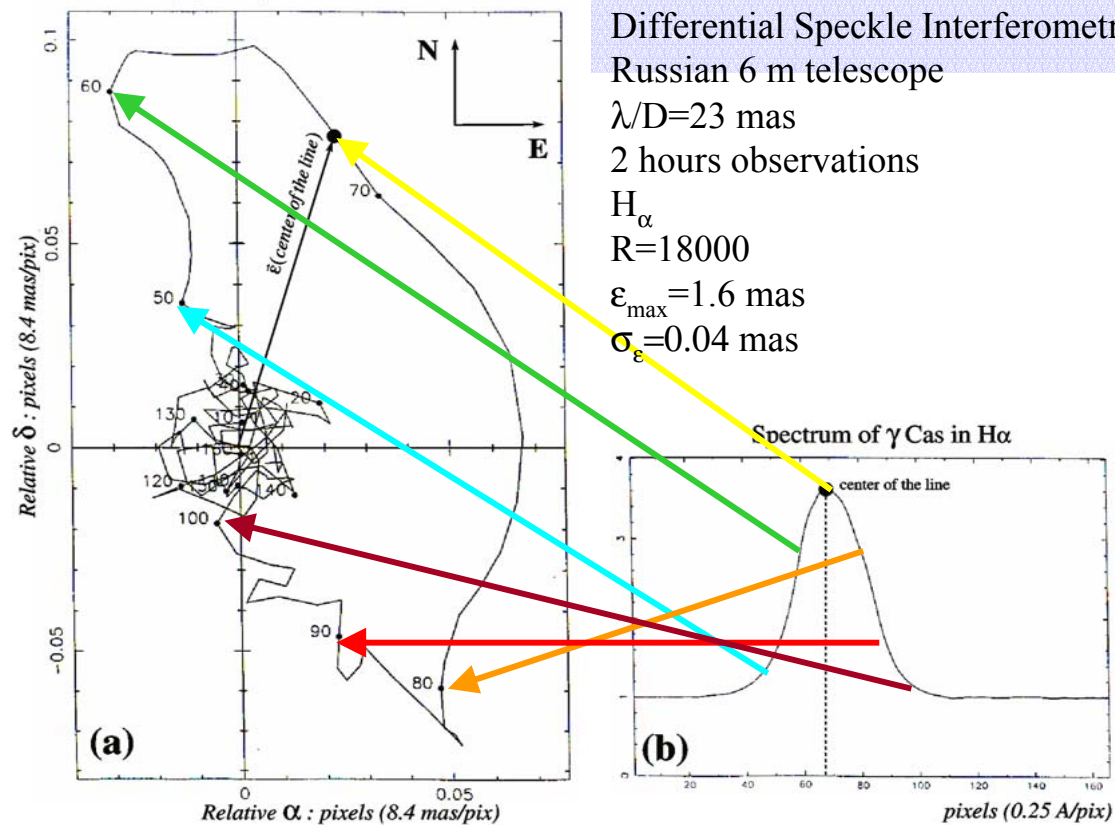


- Constant rotation
  - - - Keplerian rotation
  - · · Angular momentum conservation
- Rotation axis

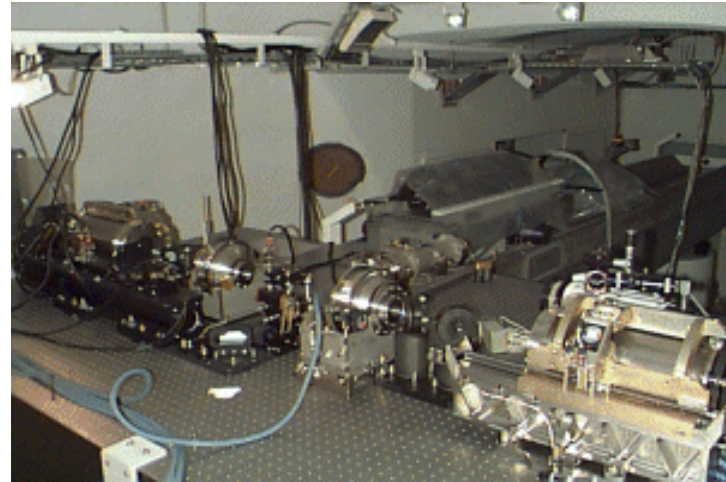
$\gamma$  Cas: Keplerian rotation

# Differential speckle interferometry of $\gamma$ Cas: $\phi=f(\lambda)$

$\bar{\epsilon}(\lambda)$  for  $\gamma$  Cas in the H $\alpha$  line

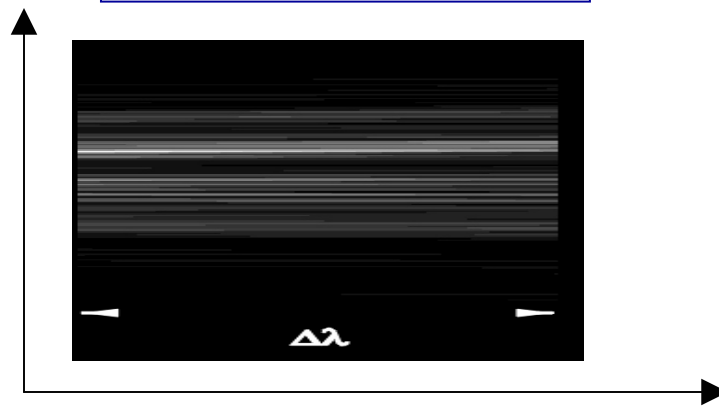


# GI2T interferometer



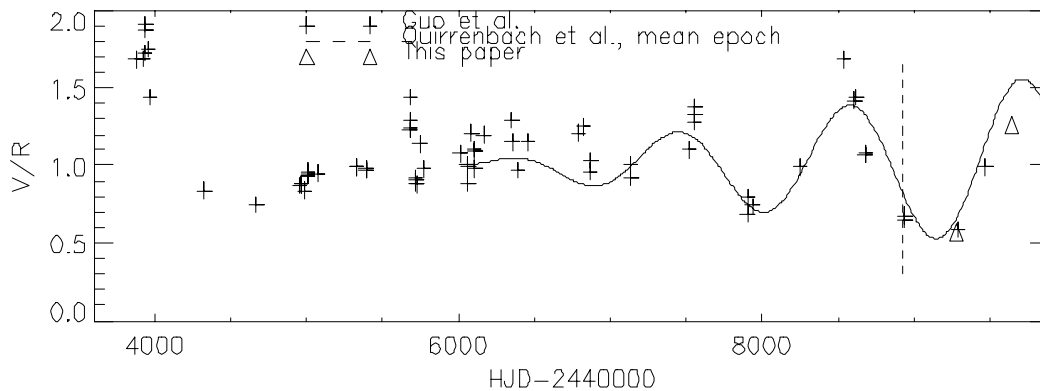
Dispersed fringes

Spatial direction  
(1 mas)

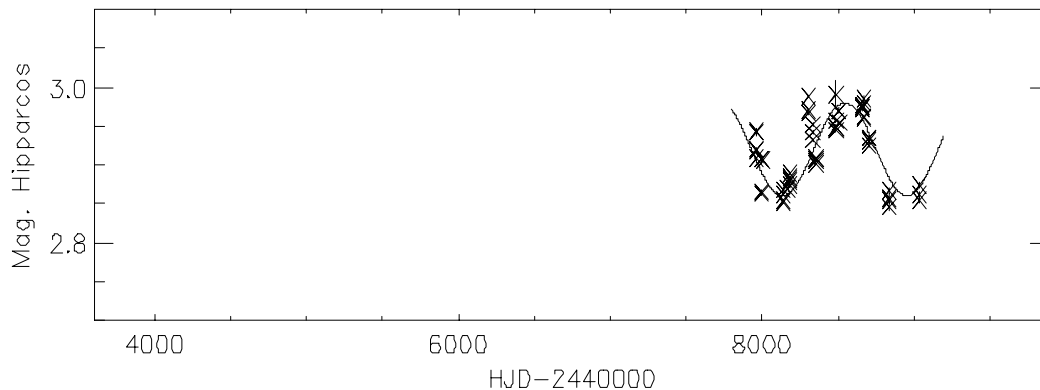


Spectral resolution (up to 0.2 Å)

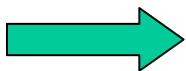
# « One-armed » oscillations in the Be Shell star $\zeta$ Tau



- Long Term H $\alpha$  Variability of  $\zeta$  Tau from Guo et al. (+) and GI2T ( $\Delta$ ) Spectroscopy
- Oscillation Curve = Sine Wave Amplifying after 1988, P=3.1 y
- Vertical Dashed Line : Mark III Observations of  $\zeta$  Tau

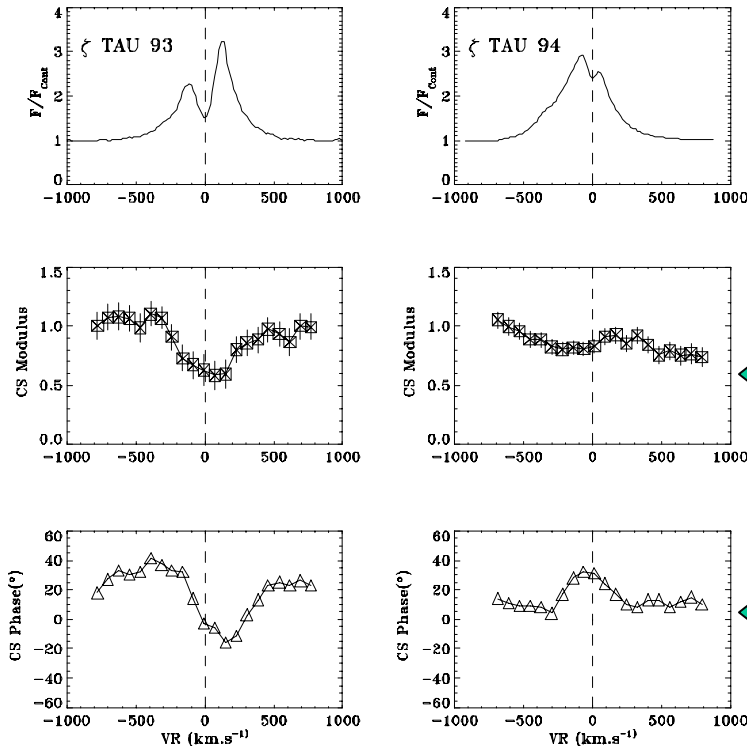


- Photometric Data from Hipparcos Mission



Note that the star became brighter just at the V/R minimum corresponding to GI2T observations in November 1993

# Interpretation of GI2T observations



H $\alpha$  GI2T Profiles Versus Doppler-shift for 93 and 94 Observations of  $\zeta$  Tau

Fringe Amplitude and Phase Diagrams

← CS Modulus

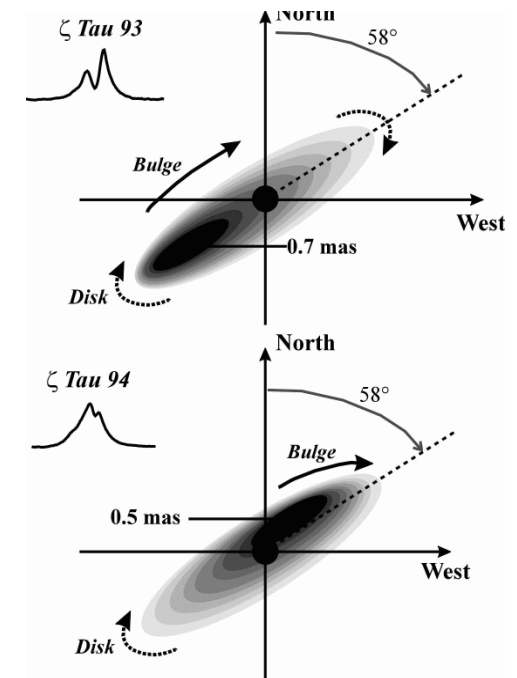
← CS Phase

Schematic Representation of  $\zeta$  Tau H $\alpha$  long Term Variability According to GI2T.

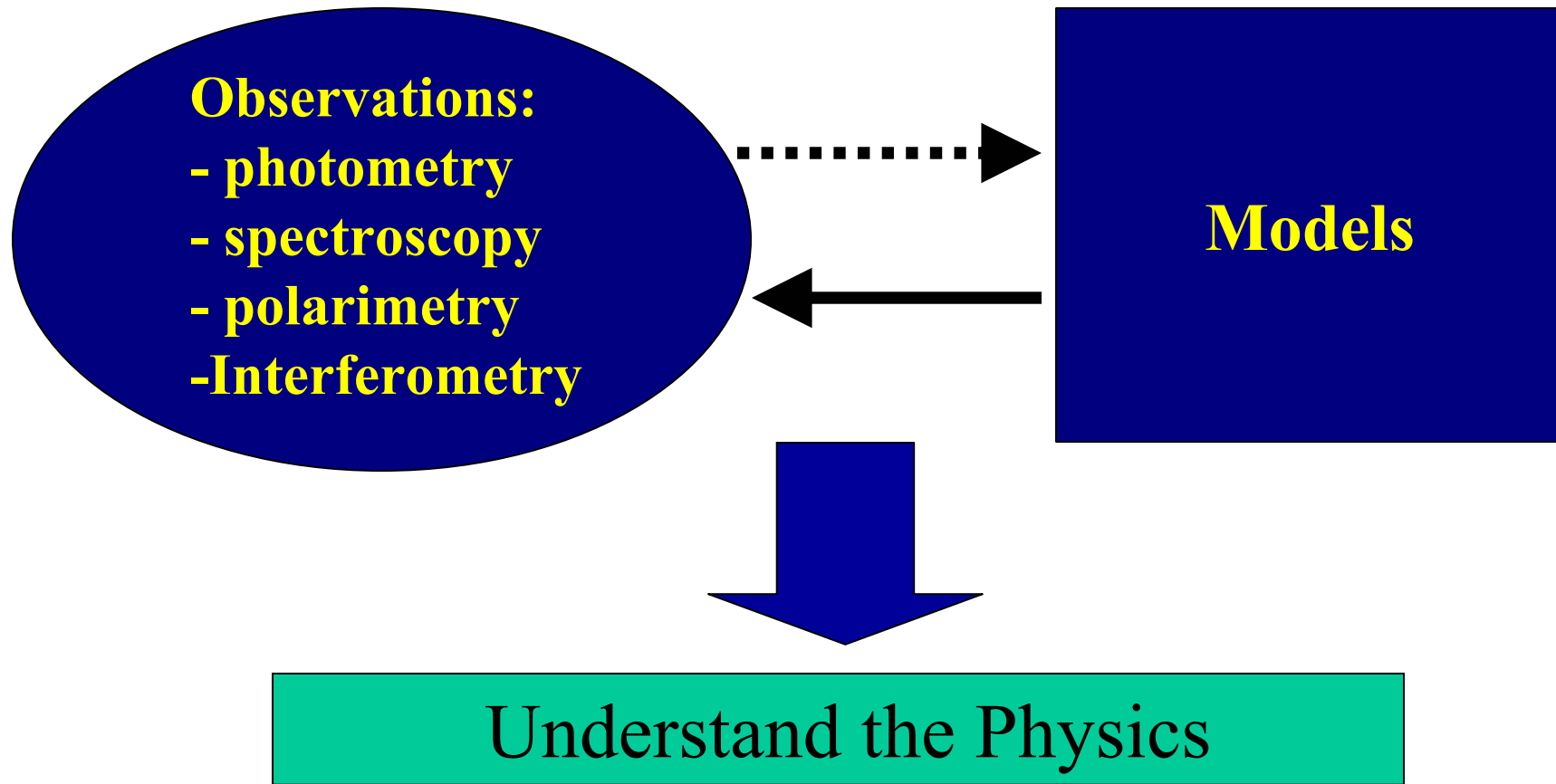
Nov. 93 : H $\alpha$  Emission with  $V/R=0.57$  and Originates in a Region of the Envelope whose N-S Projected Position is at 0.7 mas South of the Star

Oct. 94 :  $V/R=1.26$ , N-S Projected Position at 0.5 mas North of the Star

➡ Rotation of the Bulge in the Equatorial Disk of  $\zeta$  Tau



# Interferometry needs models...

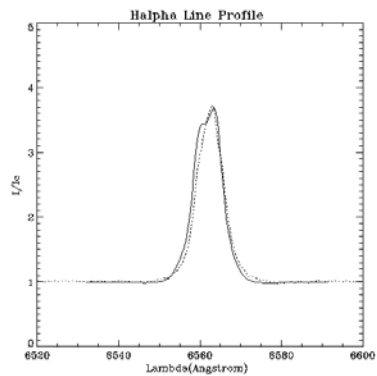


**Models need interferometry!**

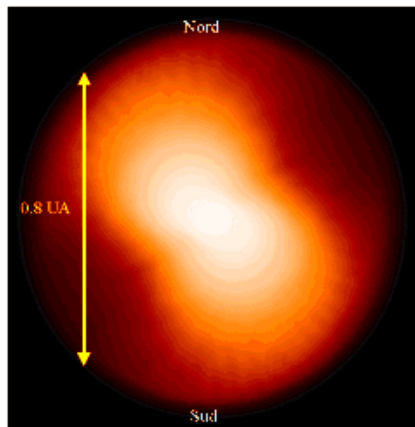


# Models: to be quantitative...

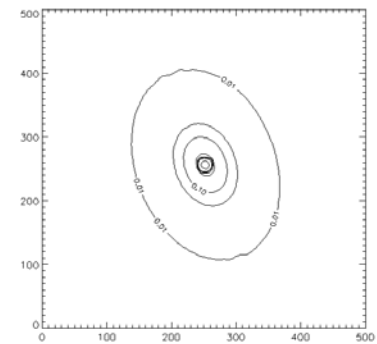
Parameters	
Spectral type	B0.5IVe
Effective temperature	25000 K
Mass	16 $M_{\odot}$
Radius	10 $R_{\odot}$
Stellar angular diameter	0.45 mas
Luminosity	$3.5 \cdot 10^4 L_{\odot}$
$V \sin i$	230 $\text{km s}^{-1}$
Inclination angle $i$	$45^{\circ}$
Results	
Polar terminal velocity	2016 $\text{km s}^{-1}$
Polar mass flux	$1.7 \cdot 10^{-9} M_{\odot} \text{ yr}^{-1} \text{ sr}^{-1}$
Equatorial terminal velocity	200 $\text{km s}^{-1}$
Equatorial mass flux	$5.1 \cdot 10^{-8} M_{\odot} \text{ yr}^{-1} \text{ sr}^{-1}$
Mass loss rate	$3.2 \cdot 10^{-7} M_{\odot} \text{ yr}^{-1}$
H $\alpha$ major axis	17 stellar radii
H $\alpha$ oblateness	0.72
H $\alpha$ extension	4 mas
Mass of the disk	$6.4 \cdot 10^{-8} M_{\odot}$



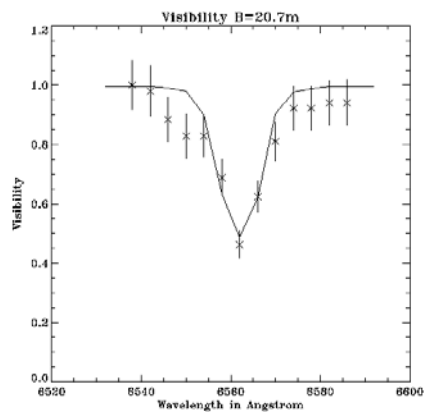
**Line profile**



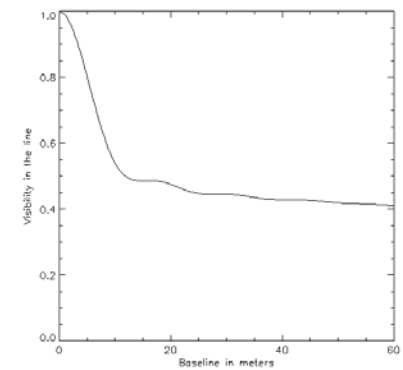
**Map in spectral line**



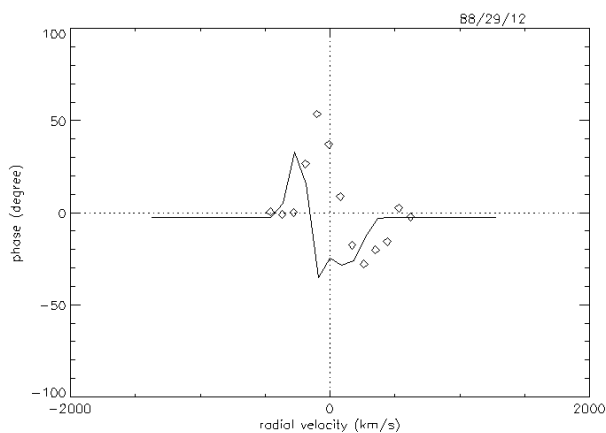
**Map in continuum**



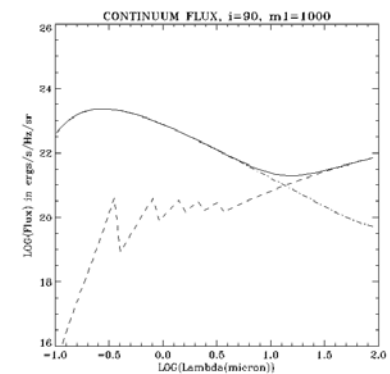
**$V=f(\lambda)$**



**$V=f(B)$**

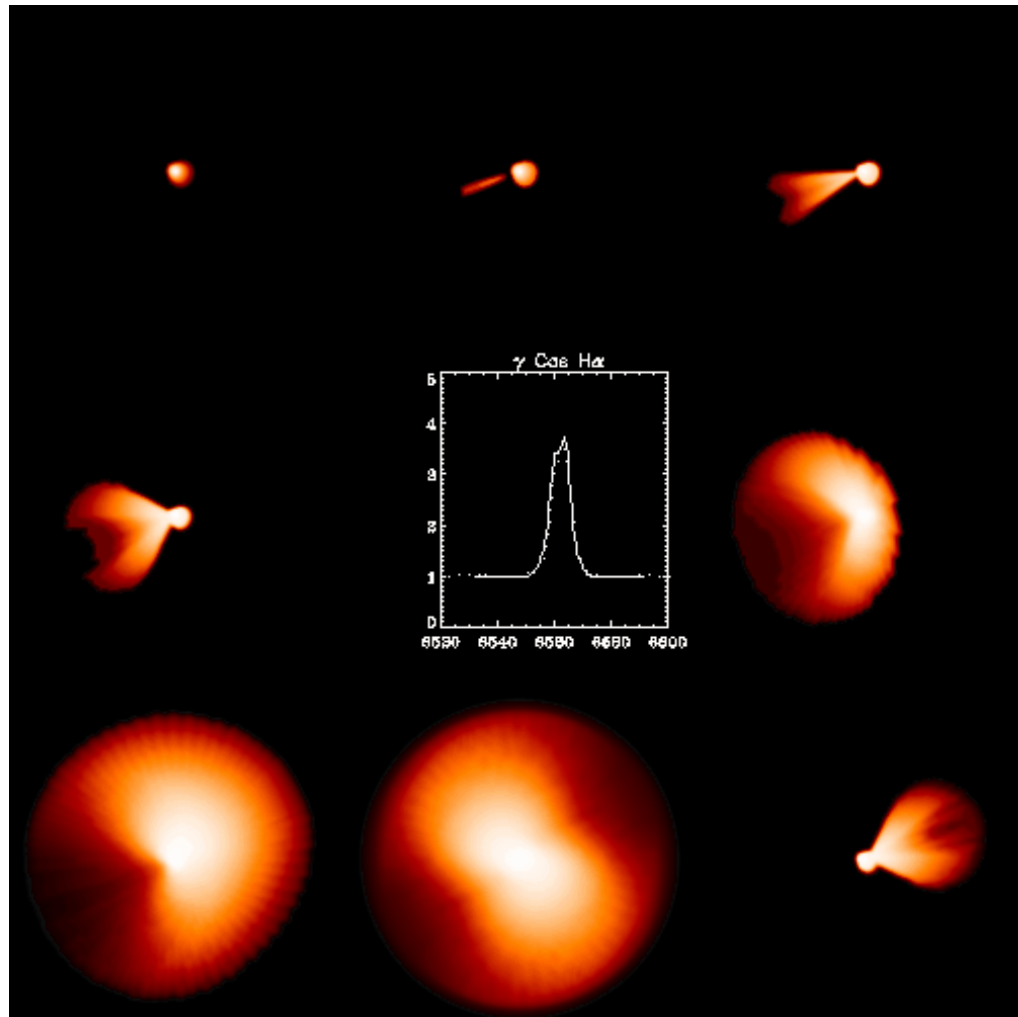


**Phase =  $f(\lambda)$**



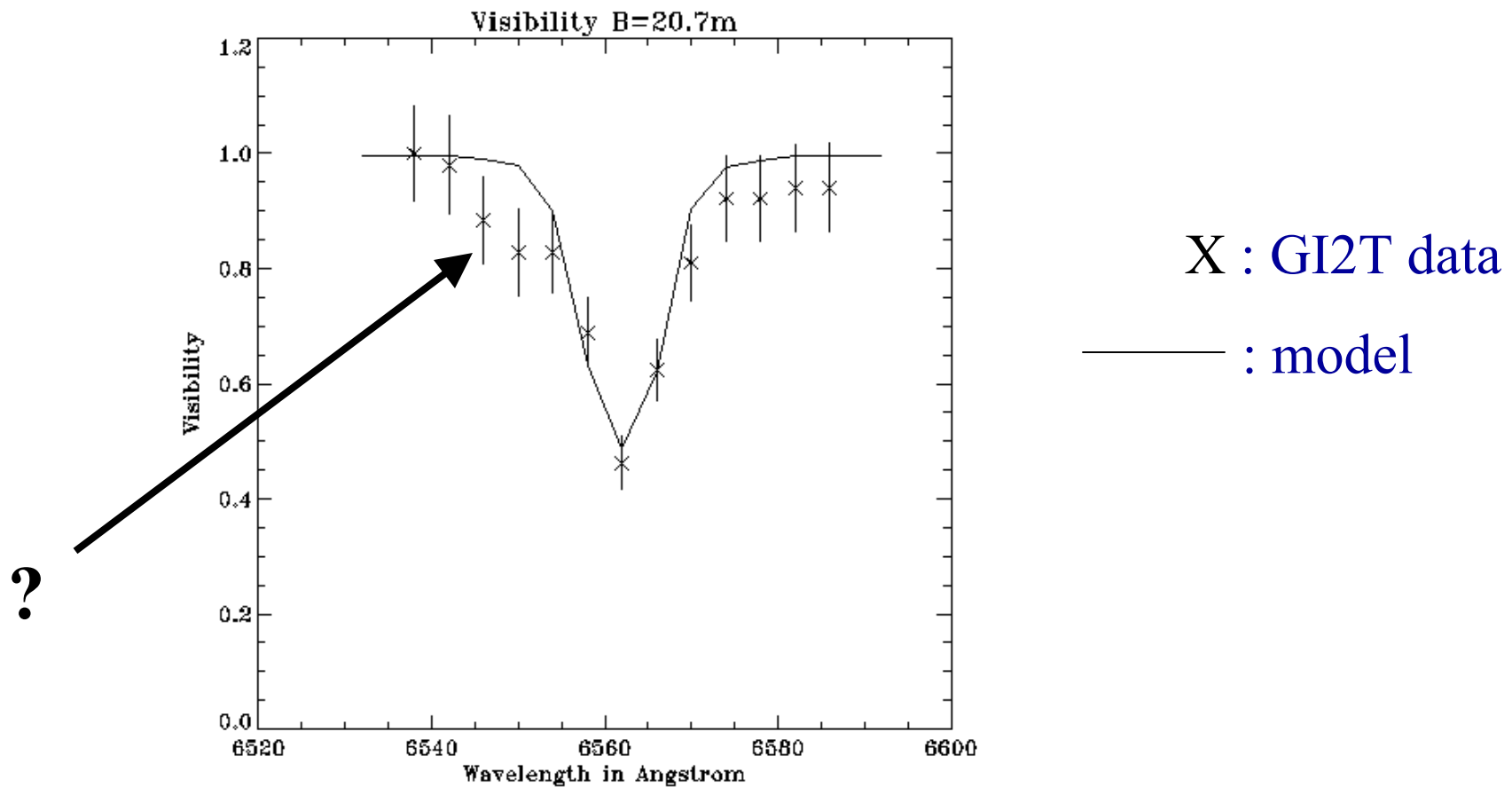
**Energy distribution**

# $\gamma$ Cas across H $\alpha$ line profile



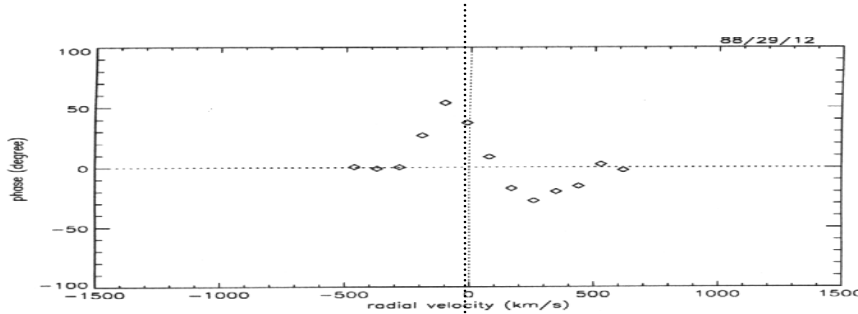
Stee et al. 1995, A&A, 300, 219

# Can HARO put constraints on these maps ?

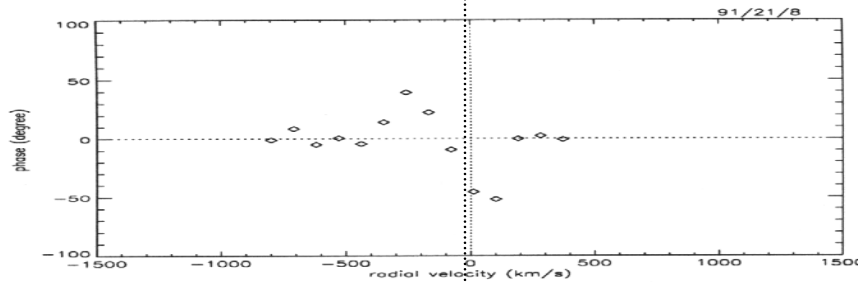


# $\gamma$ Cas « one-armed » oscillations: $\phi = f(t)$

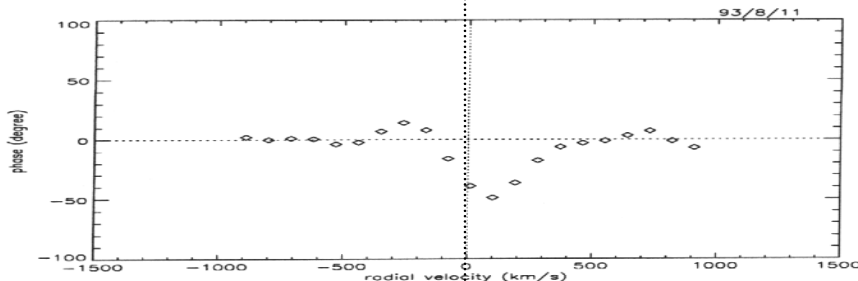
88  
V>R



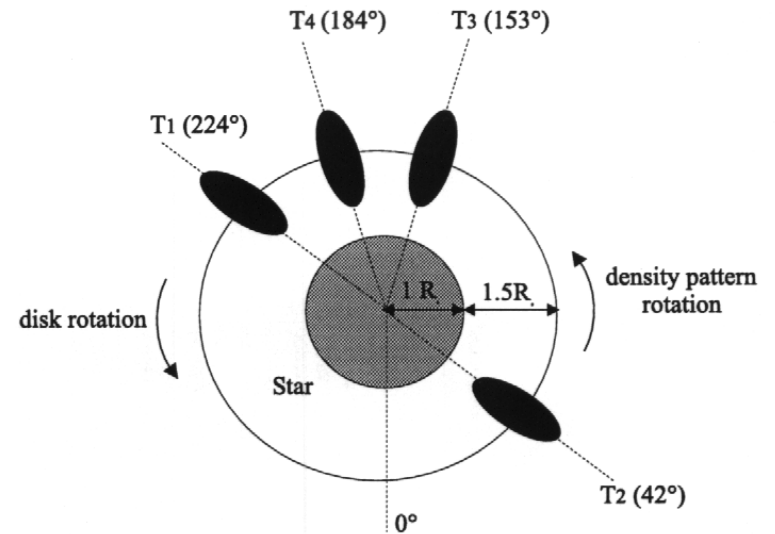
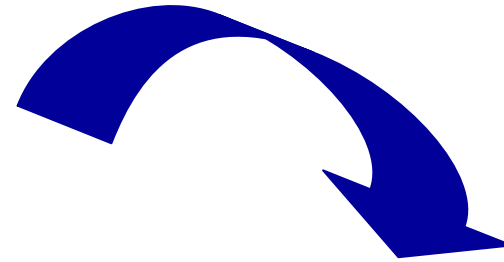
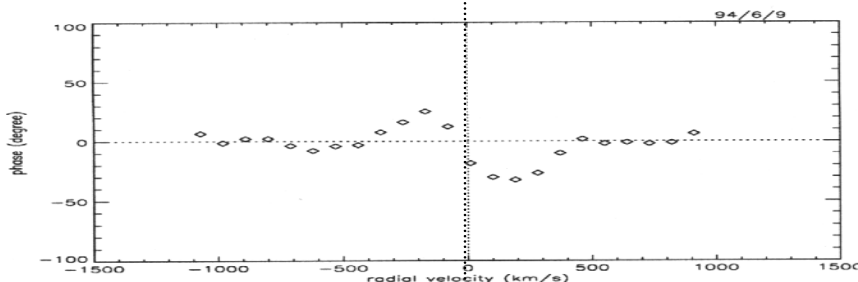
91  
V<R



93  
V<R



94  
V<R

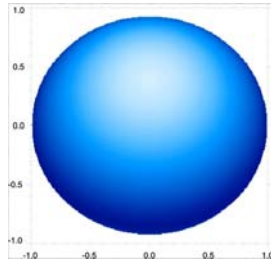


High density pattern in  $\gamma$  Cas equatorial disk

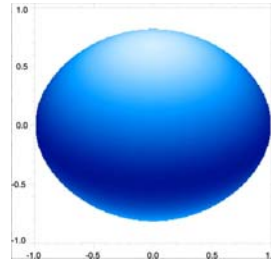
Berio et al. 1999, A&A, 345, 203

# Stellar rotation $|v| = f(B)$

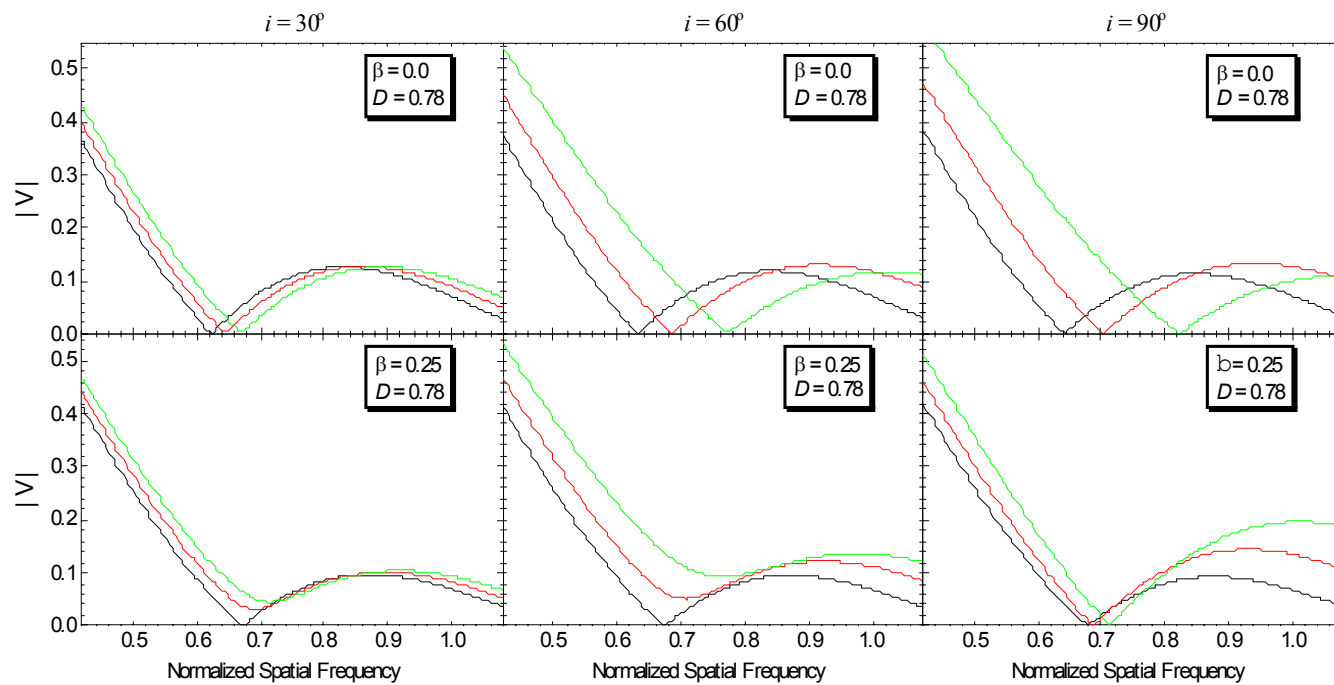
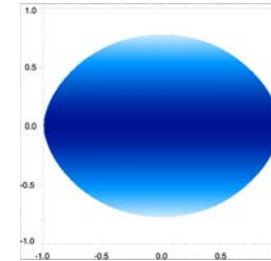
$i = 30^\circ$



$i = 60^\circ$

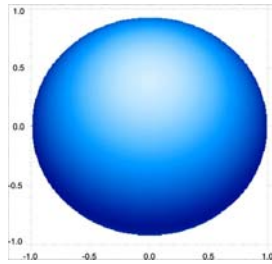


$i = 90^\circ$

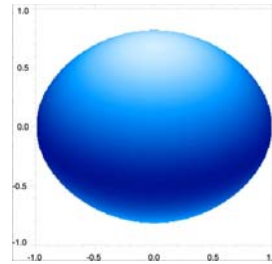


# Stellar rotation $\phi = f(B)$

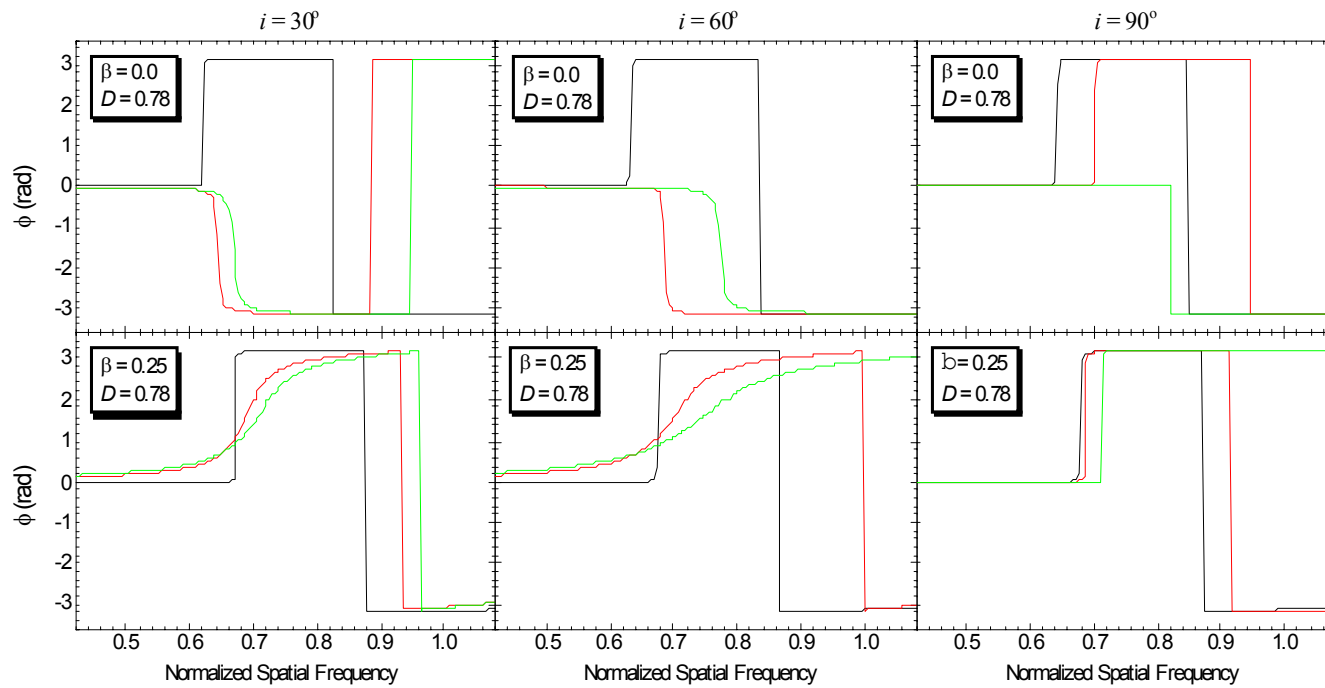
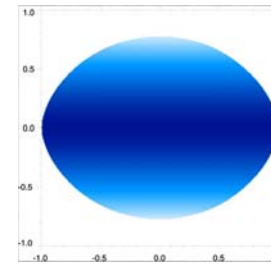
$I = 30^\circ$



$i = 60^\circ$



$i = 90^\circ$



# Differential interferometry

- Very accurate
  - High precision
  - Access to very small detail  $\approx \mu\text{m}$
  - Put very strong constraints
- 
- Difficult to interpret
  - Be careful with resolved objects
  - Need models